

# **EECS 240**

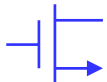
# **Analog Integrated Circuits**

## **Lecture 8: References**

**Ali M. Niknejad and Bernhard E. Boser**

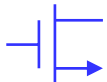
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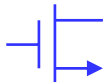
# Outline

- Objectives
- CMOS implementations
- Startup circuits
- Typical performance
- Constant  $XXX$  references

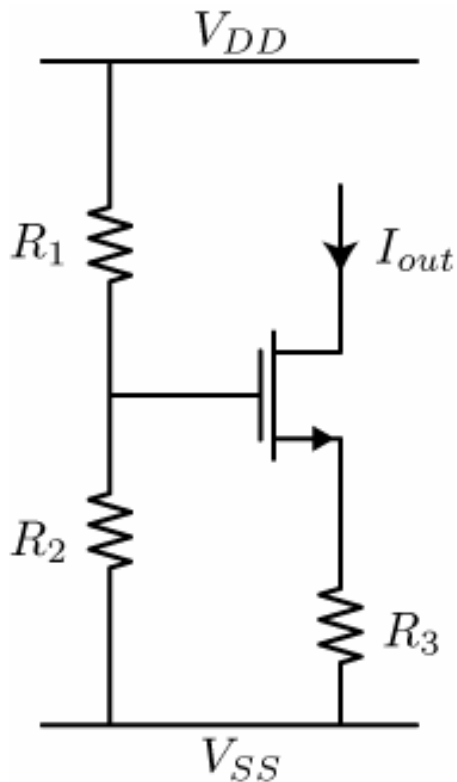


# References

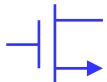
- Applications
  - Bias current
  - ADC / DAC references
- Solutions
  - Voltage references:
    - PTAT ( $V_t = kT/q$ )
    - Bandgap
    - Threshold voltage,  $V_{TH}$ ,  $\Delta V_{TH}$
  - Special purpose:
    - Constant  $g_m$
  - No “direct” current reference
- Specifications
  - Accuracy:  $\sigma$  of  $\Delta V_{out}/V_{out}$
  - Temperature coefficient,  $TC_F$
  - Power rejection ratio, PSRR
  - Trimming
  - Supply voltage
  - Power dissipation



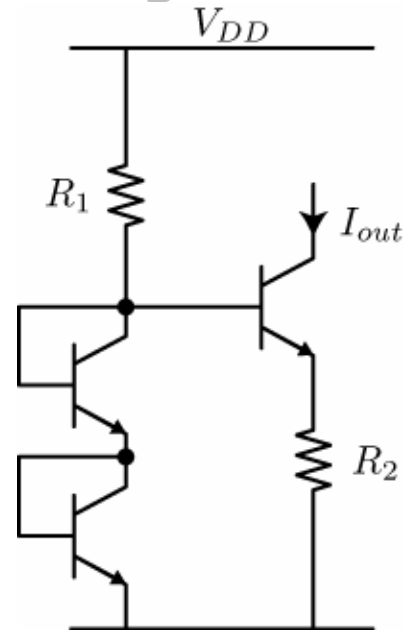
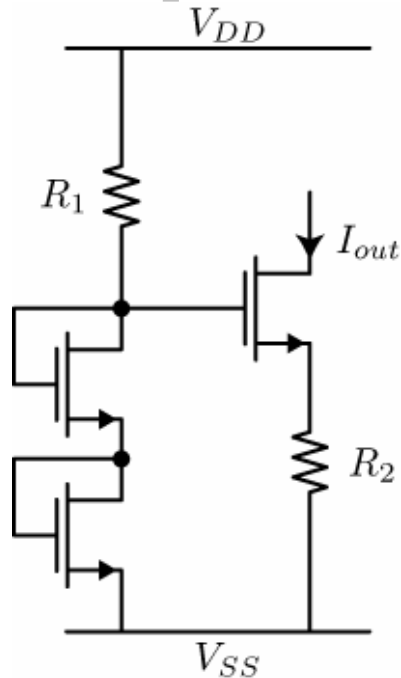
# Supply Dependent Biasing



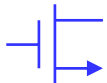
- Okay for test circuits, especially if resistors are off-chip. But output current is inaccurate and varies with supply/temperature.
- Realization of small (nA) currents requires big resistors (too much area).



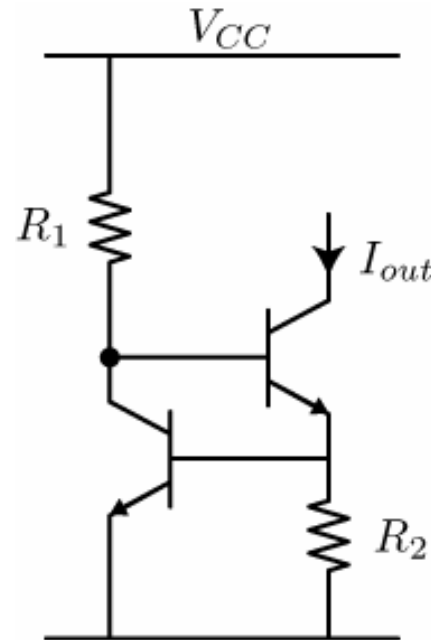
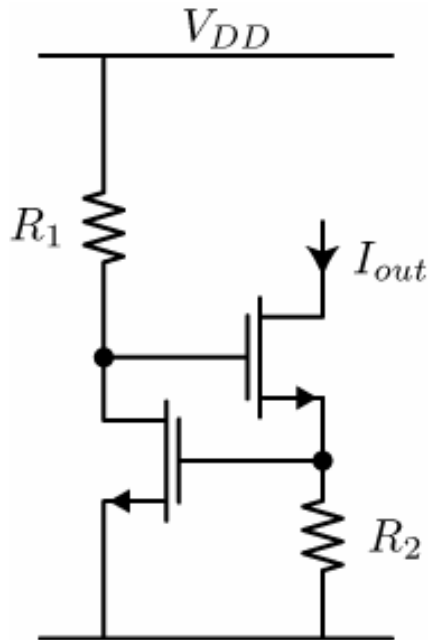
# Simple Supply Rejection



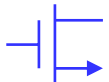
- Use a  $V_{GS}$  or even better a  $V_{BE}$  as a reference.  $V_{BE}$  is very insensitive (logarithmically) to current variations.



# Improved $V_{GS}/V_{BE}$ Reference



- Now we have only one  $V_{BE}$  ( $V_{GS}$ ) as the reference. If the overdrive of the MOS is small relative to  $V_T$ , this is a threshold reference.



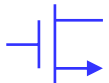
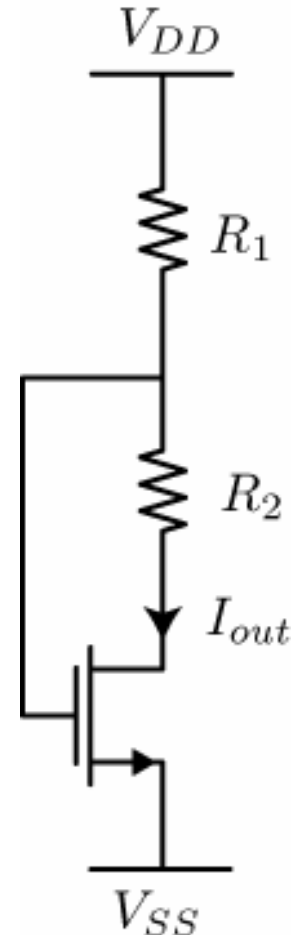
# Peaking Current Source

$$V_o = V_{GS} - IR_2$$

$$\frac{dV_o}{dI} = \frac{dV_{GS}}{dI} - R_2$$

$$\frac{dV_o}{dI} = \frac{1}{g_m} - R_2 = 0 \quad R_2 = \frac{1}{g_m}$$

- Useful for very small (nA) current levels.
- Can compensate for variations in  $V_{GS}$  with a resistor to produce first order supply independent.

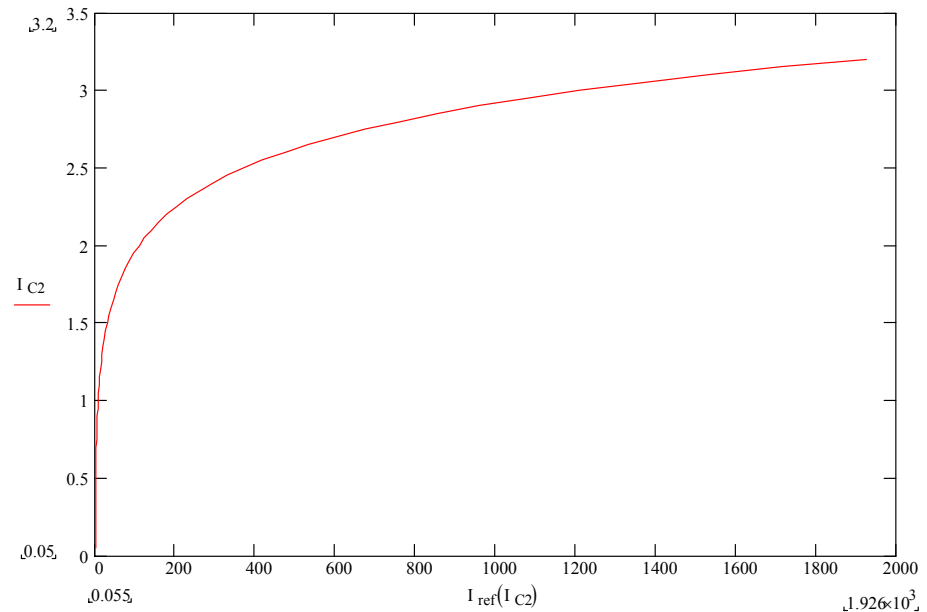
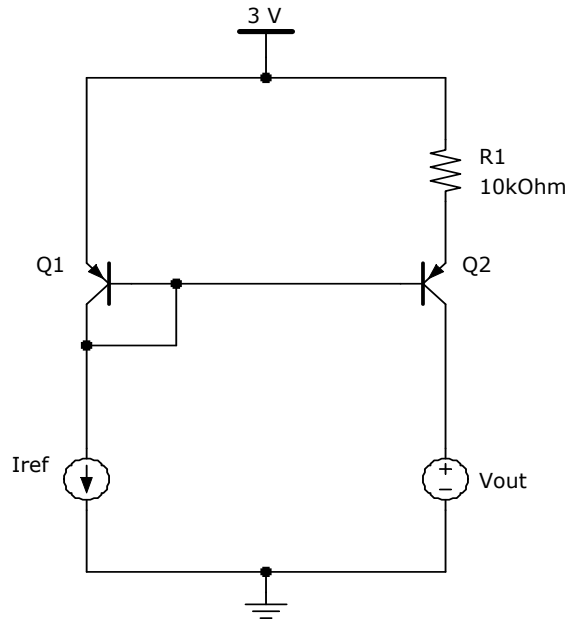


# Widlar Reference

**DC Analysis** DC1

Device Iref

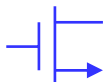
sweep from 0 to 300u (200 steps)



$$V_{BE1} = V_{BE2} + R_1 I_{C2}$$

$$V_t \ln\left(\frac{I_{ref}}{I_{s1}}\right) = V_t \ln\left(\frac{I_{C2}}{I_{s2}}\right) + R_1 I_{C2}$$

- $I_{C2}$  is “relatively” insensitive to  $I_{ref}$
- $\rightarrow$  first order supply independence



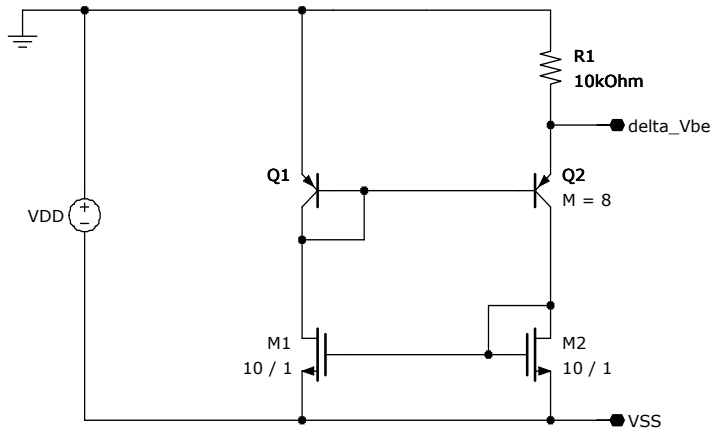


# PTAT Reference

DC AnalysisDC1

Device VDD

sweep from 10m to 3 (199 steps)



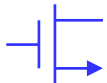
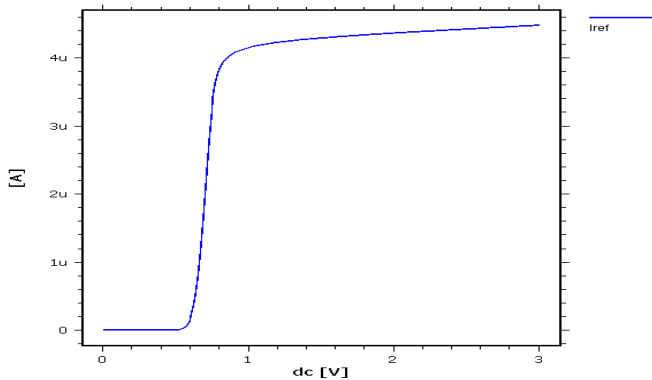
$$\Delta V_{BE} = V_t \ln \left( \frac{I_{s2}}{I_{s1}} \frac{I_{C1}}{I_{C2}} \right)$$

$$= V_t \ln \left( M \frac{I_{C1}}{I_{C2}} \right)$$

$$\propto T$$

Issues:

- Cascoding
- Self-biasing
- Temperature Coefficient
- Vertical BJT
- Startup



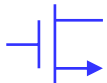
# Temperature Coefficient

TC of Reference Voltage:

$$\begin{aligned}TC_F &= \frac{1}{\Delta V_{BE}} \frac{d\Delta V_{BE}}{dT} \\&= \frac{1}{\Delta V_{BE}} \frac{\Delta V_{BE}}{T} \\&= \frac{1}{T} \\&\cong 3300\text{ppm/K} \quad \text{at room temperature (300° K)}\end{aligned}$$

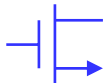
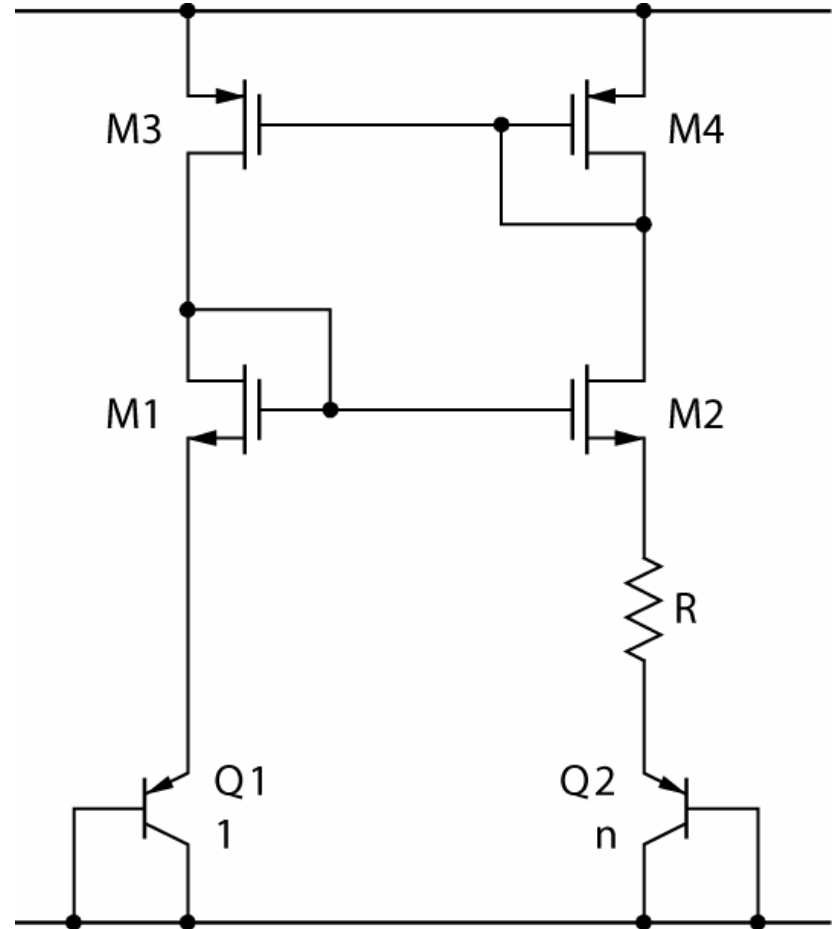
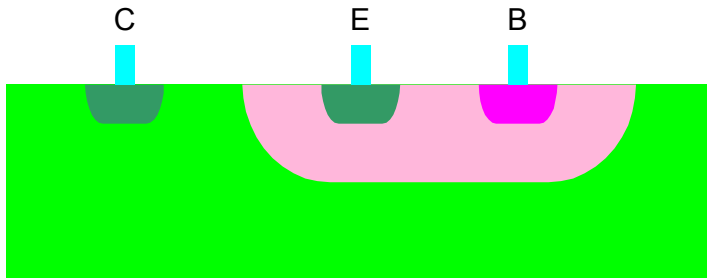
TC of Reference Current:

$$\begin{aligned}I_{out} &= \frac{\Delta V_{BE}}{R_1} \\TC_F &= \frac{1}{I_{out}} \frac{dI_{out}}{dT} \\&= \frac{1}{\Delta V_{BE}} \frac{d\Delta V_{BE}}{dT} - \frac{1}{R_1} \frac{dR_1}{dT} \\&= 3300\text{ppm/K} - 1500\text{ppm/K} = 1800\text{ppm/K} \\&\quad \text{for n+ diffusion resistor}\end{aligned}$$

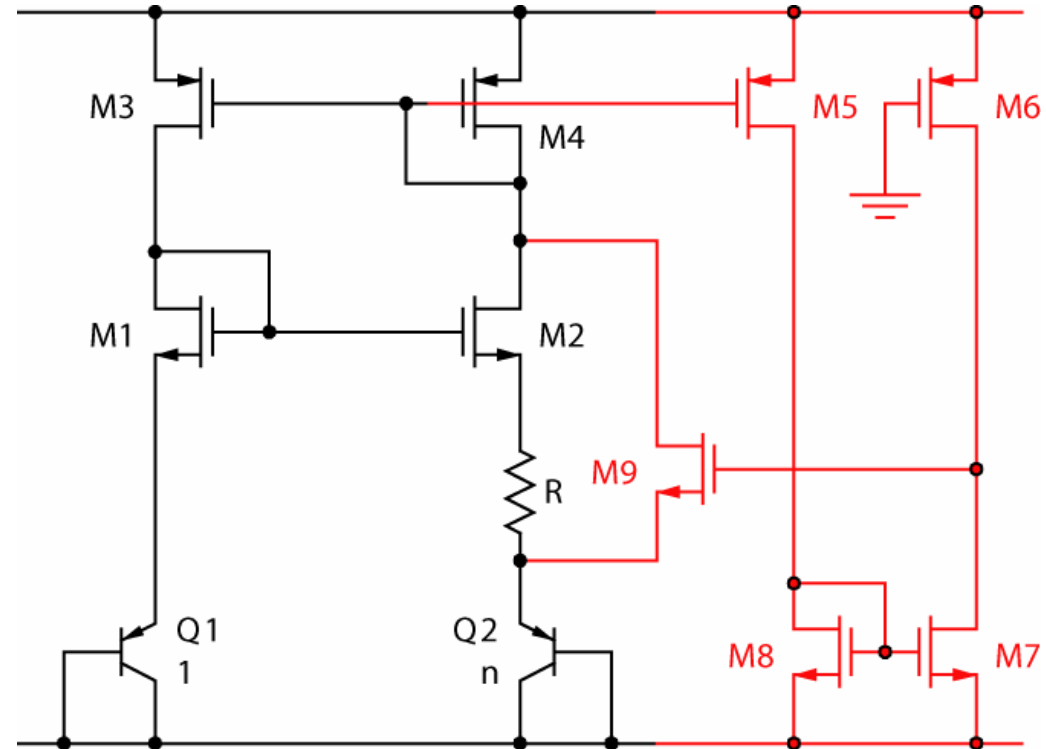
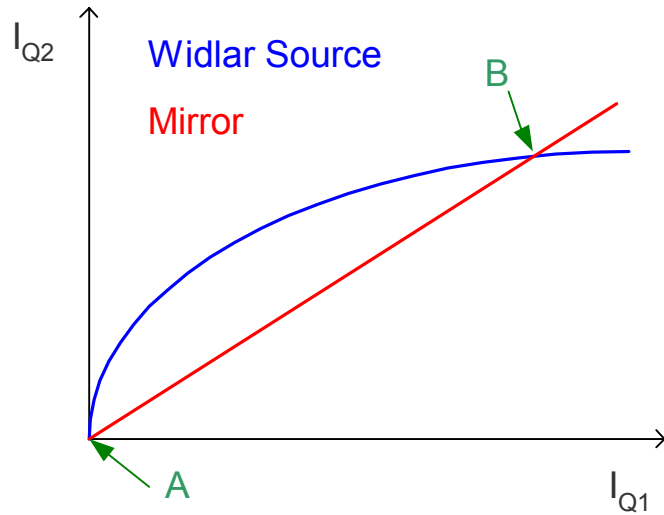


# CMOS PTAT Reference

Vertical PNP

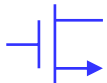


# Startup Circuit



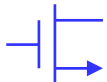
Parasitic operating point A:

- Positive feedback  $\rightarrow$  unstable
- Noise drives circuit away from A (and to B)
- Problem: gain at A too small ( $I_Q = 0$ )

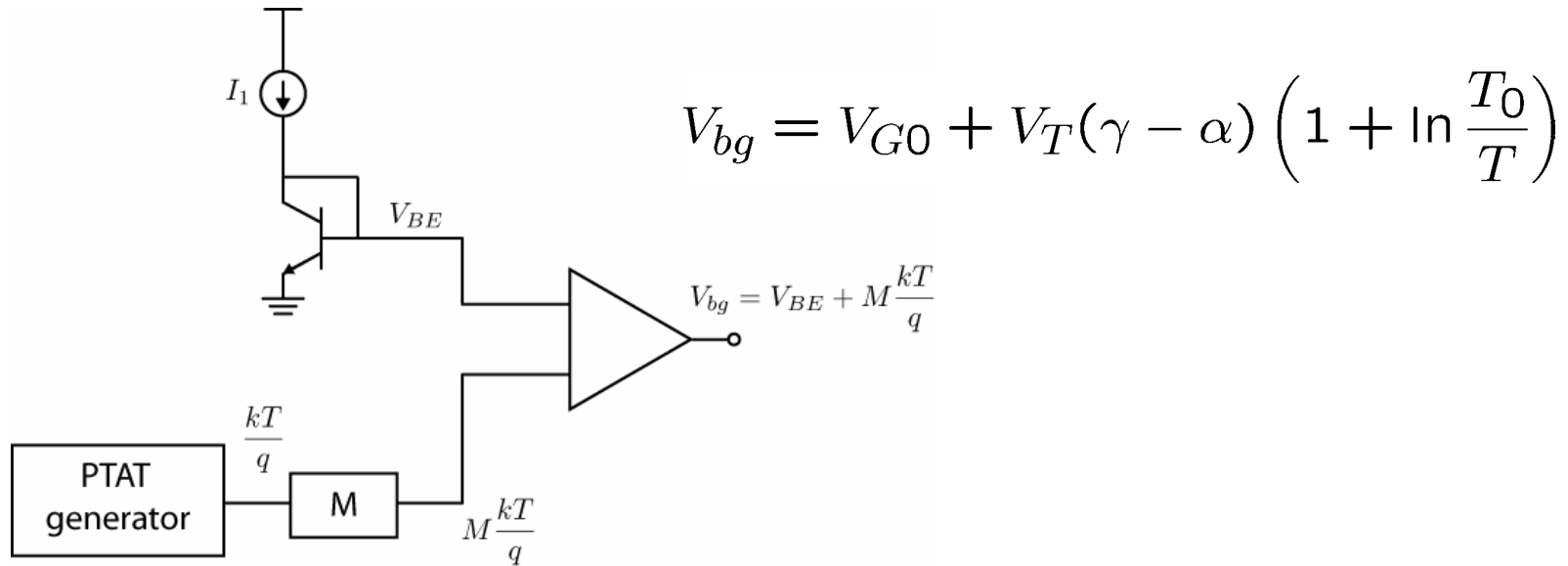


# Bandgap Reference

- Supply and temperature insensitive
- $V_{\text{BG,Si}} = 1.205\text{V}$
- Curvature correction
- References:
  - R. Widlar, JSSC 2/1971, pp. 2  
first report
  - G. Nicollini, JSSC 1/1991, pp. 41  
offset compensated amplifier
  - K. Tham, JSSC 5/1995, pp. 586  
self-regulated supply for improved PSRR
  - A. Boni, JSSC 10/2002, pp. 1339  
bandgap reference for  $V_{\text{DD}} < V_{\text{BG}}$
  - P. Malcovati, JSSC 7/2001, pp. 1076  
curvature corrected CMOS bandgap reference

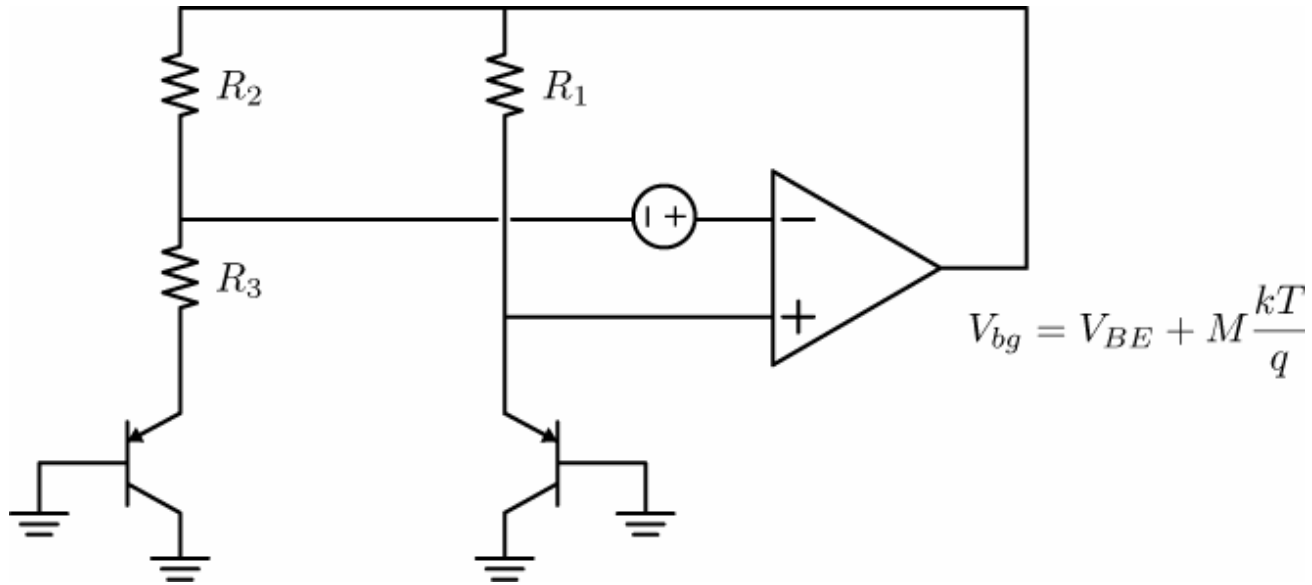


# Hypothetical Band-Gap



- $V_{BE}$  has a tempco of  $-2 \text{ mV}/^\circ\text{C}$ . If we add this to a multiple of the thermal voltage with positive tempco of  $0.085 \text{ mV}/^\circ\text{C}$ , we can achieve temperature independence.

# “CMOS” Bandgap



$$V_{R3} = V_{EB1} - V_{EB2} + V_{OS} = \Delta V_{EB} + V_{OS}$$

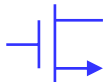
$$V_{R2} = \frac{R_2}{R_3} V_{R3} = \frac{R_2}{R_3} (\Delta V_{EB} + V_{OS})$$

$$V_{BG} = \left( 1 + \frac{R_2}{R_3} \right) (\Delta V_{EB} + V_{OS}) + V_{EB2}$$



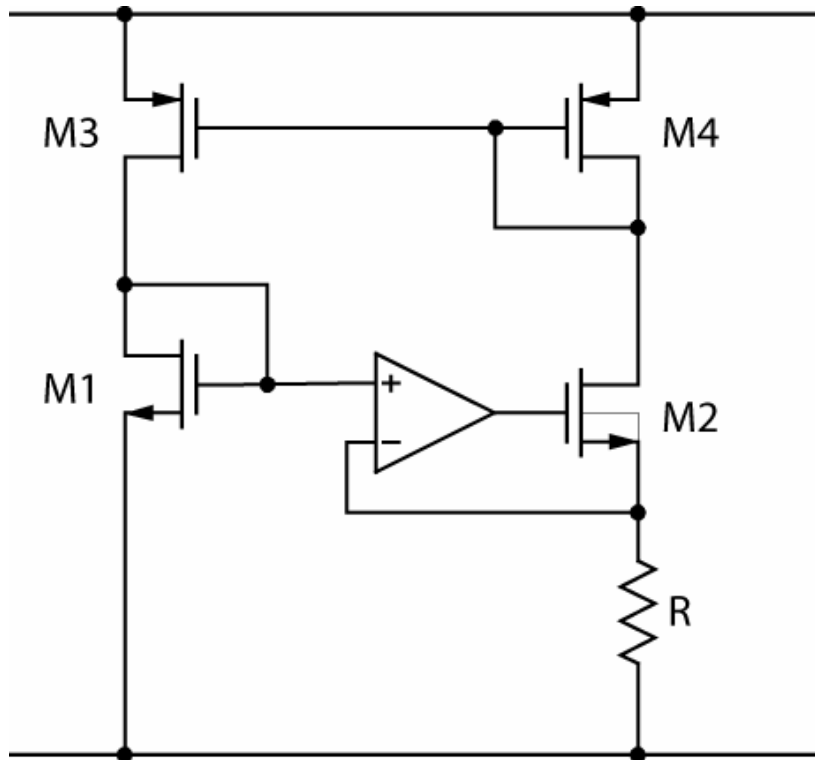
# Bandgap Performance

	[Nicollini]	[Tham]	[Malcovati]
Supply	+/- 5V	3V	1V
Output voltage	6.2V	1.24V	0.54V
Accuracy ( $\sigma$ )	24mV	20mV	
$TC_F$	15ppm/°C	85ppm/°C	7.5ppm/°C
PSRR	86dB	80dB @ 10kHz 40dB @ 500kHz	212ppm/V at DC
Power dissipation	4.8mW	1mW	92 $\mu$ W



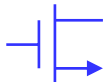


# Constant $g_m$ Reference



$$\omega_u \propto \frac{g_m}{C_L}$$

$$g_{m1} = \frac{1}{R}$$



# Reference Distribution

- Single shared reference
- Current distribution:
  - Many wires
  - Increase power dissipation
- Voltage distribution:
  - Susceptible to mismatch
  - → use large  $V_{GS}$  in distribution network
  - Careful supply routing to avoid poor PSRR
  - Avoid loops in analog supply

