

“I - T”

## Single-Stage Amplifiers

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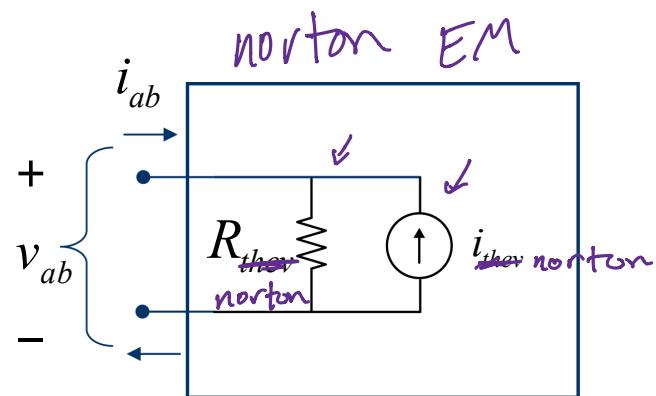
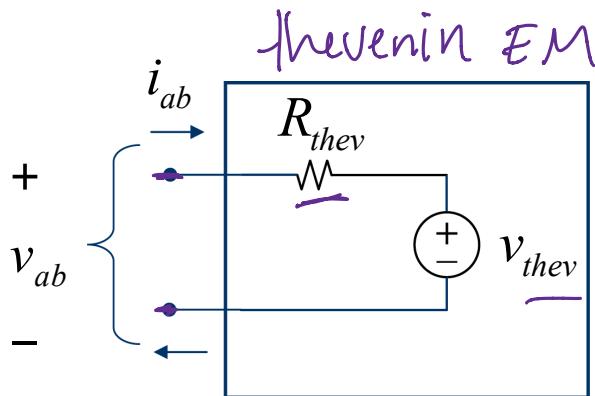
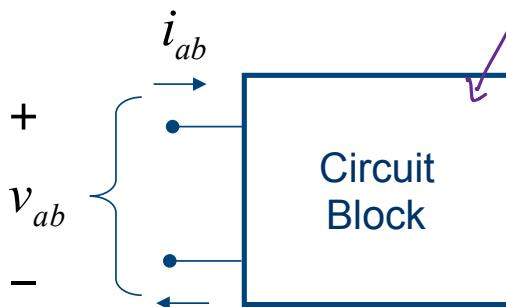
# Announcements

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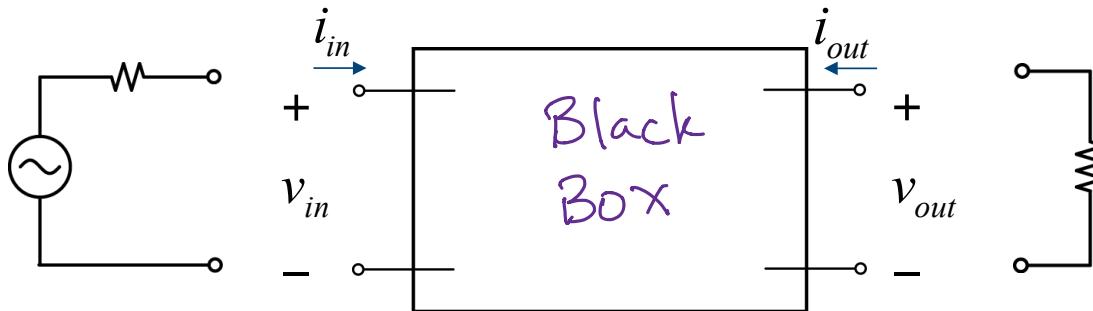
- HW8 due on Friday
  - PICK UP EXAM

# One-Port Models (EECS 16A)

- A terminal pair across which a voltage and associated current are defined

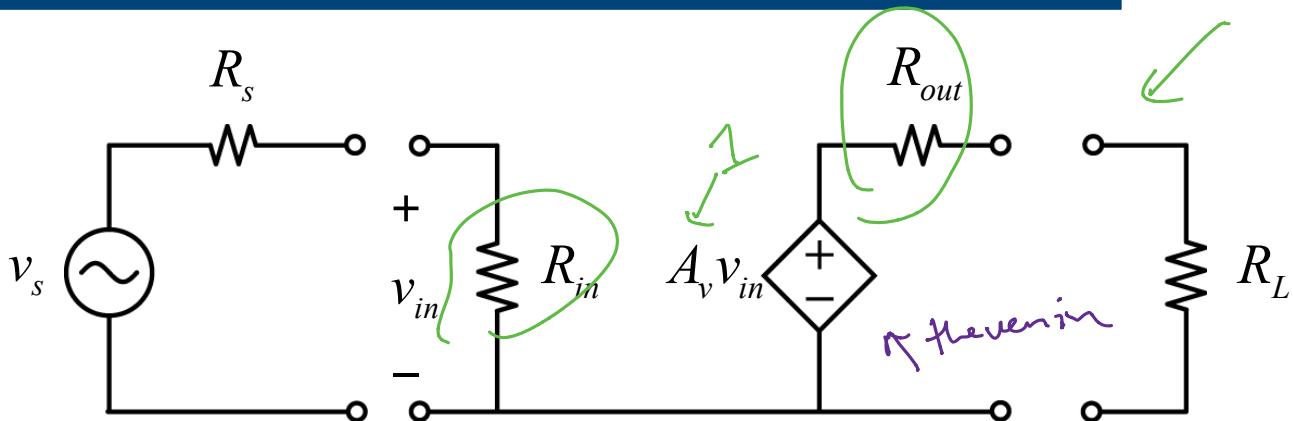


# Small-Signal Two-Port Models

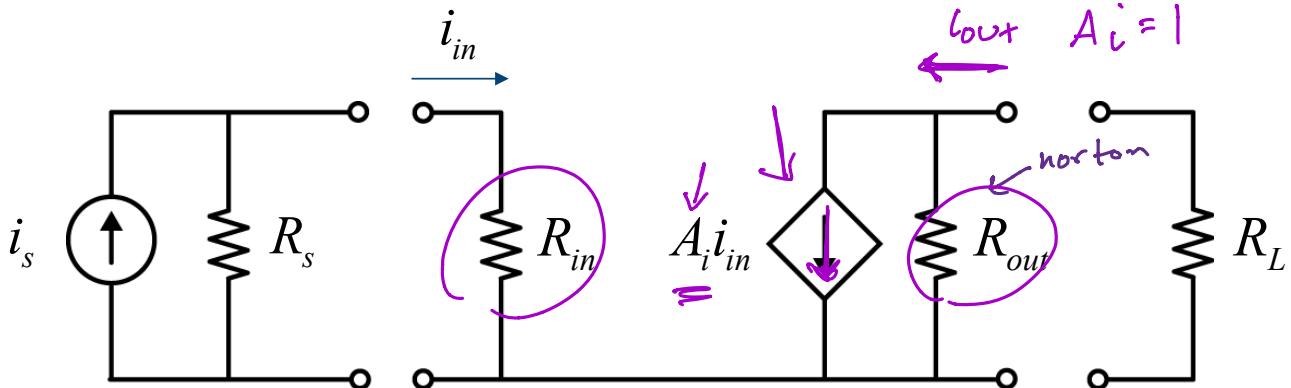


- We assume that input port is linear and that the amplifier is *unilateral*:
  - Output depends on input but input is independent of output.
- Output port : depends linearly on the current and voltage at the input and output ports
- Unilateral assumption is good as long as “overlap” capacitance is small (MOS)

# Two-Port Small-Signal Amplifiers

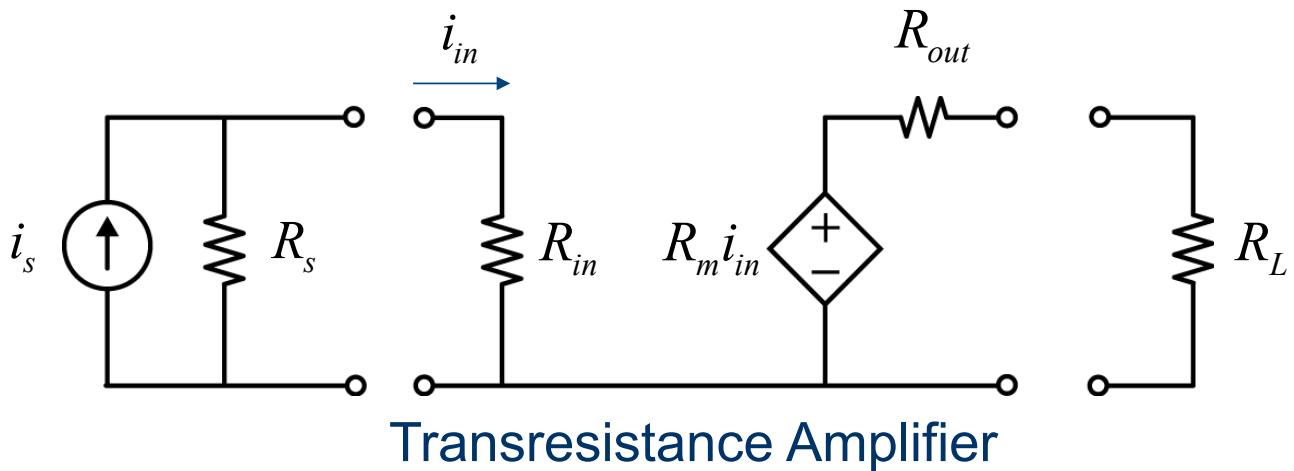
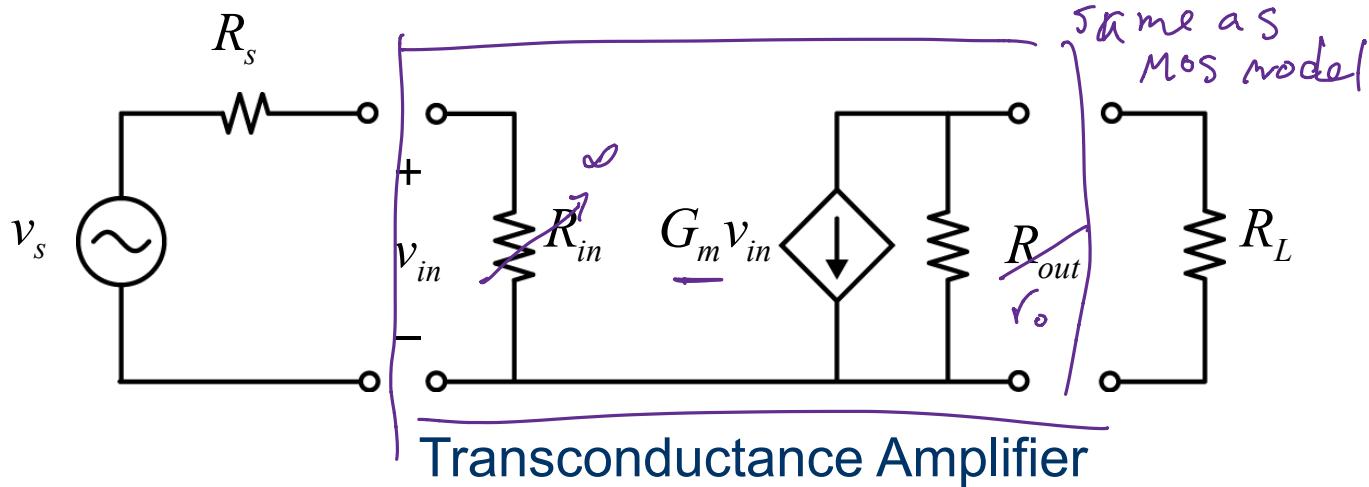


Voltage Amplifier



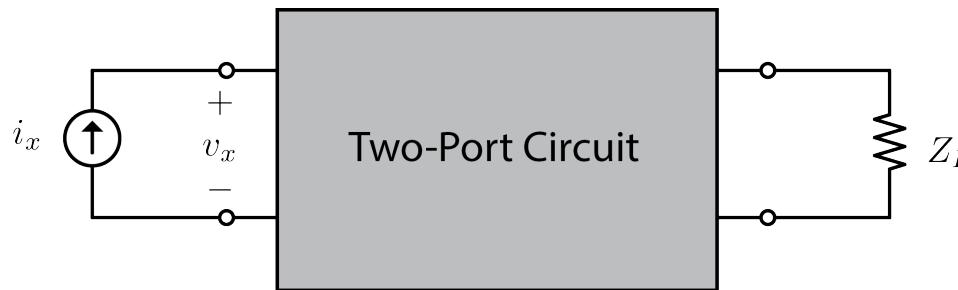
Current Amplifier

# Two-Port Small-Signal Amplifiers

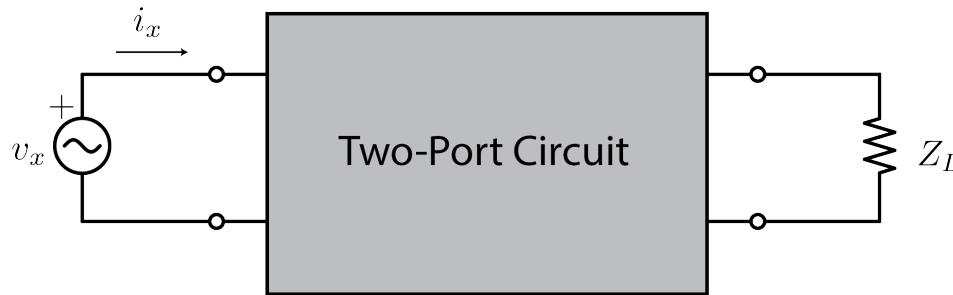


# Input Impedance $Z_{in}$

Looks like a Thevenin resistance measurement, but note that the output port has the load resistance attached



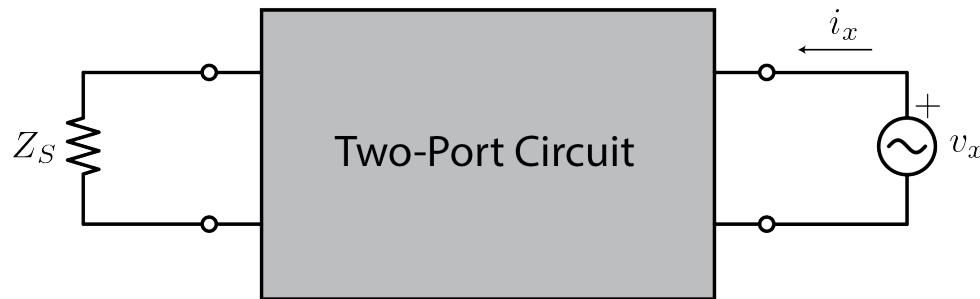
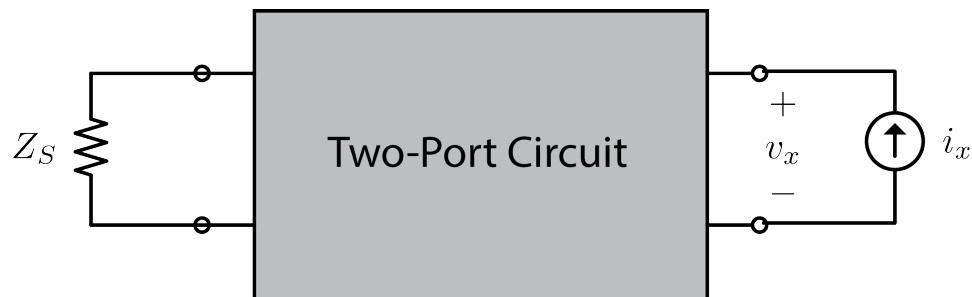
$$Z_{in} = \left. \frac{v_x}{i_x} \right|_{\substack{Z_S \text{ removed}, \\ Z_L \text{ attached}}}$$



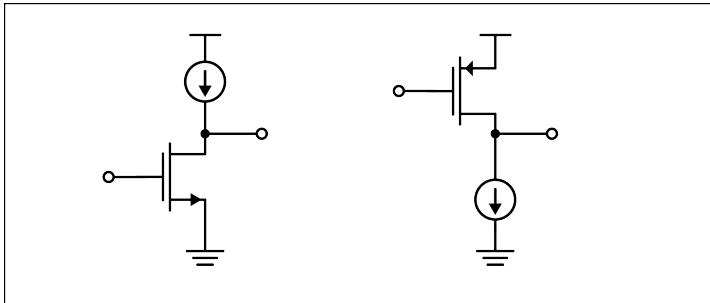
# Output Impedance $Z_{out}$

Looks like a Thevenin resistance measurement, but note that the *input* port has the *source* resistance attached

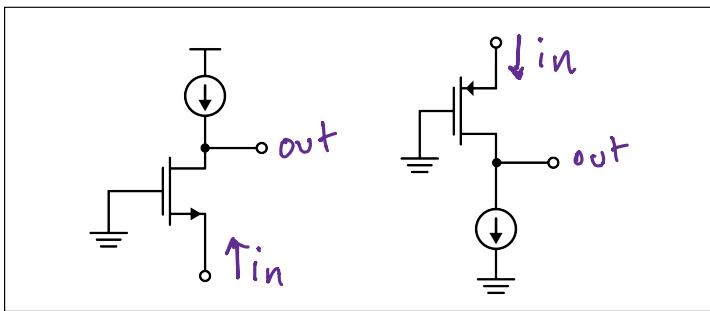
$$Z_{out} = \frac{v_x}{i_x} \Big|_{\substack{Z_L \text{ removed}, \\ Z_S \text{ attached}}}$$



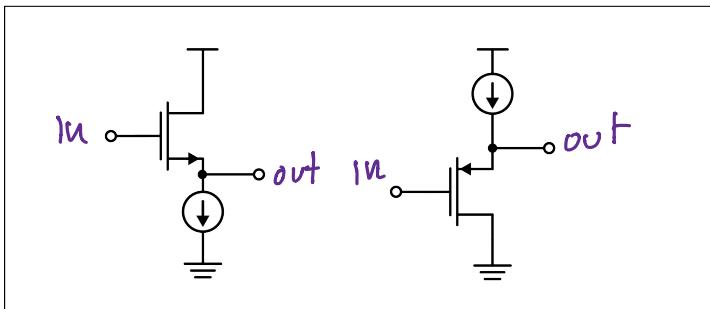
# Single-Stage Amplifier Types



Common Source (CS)



Common Gate (CG)

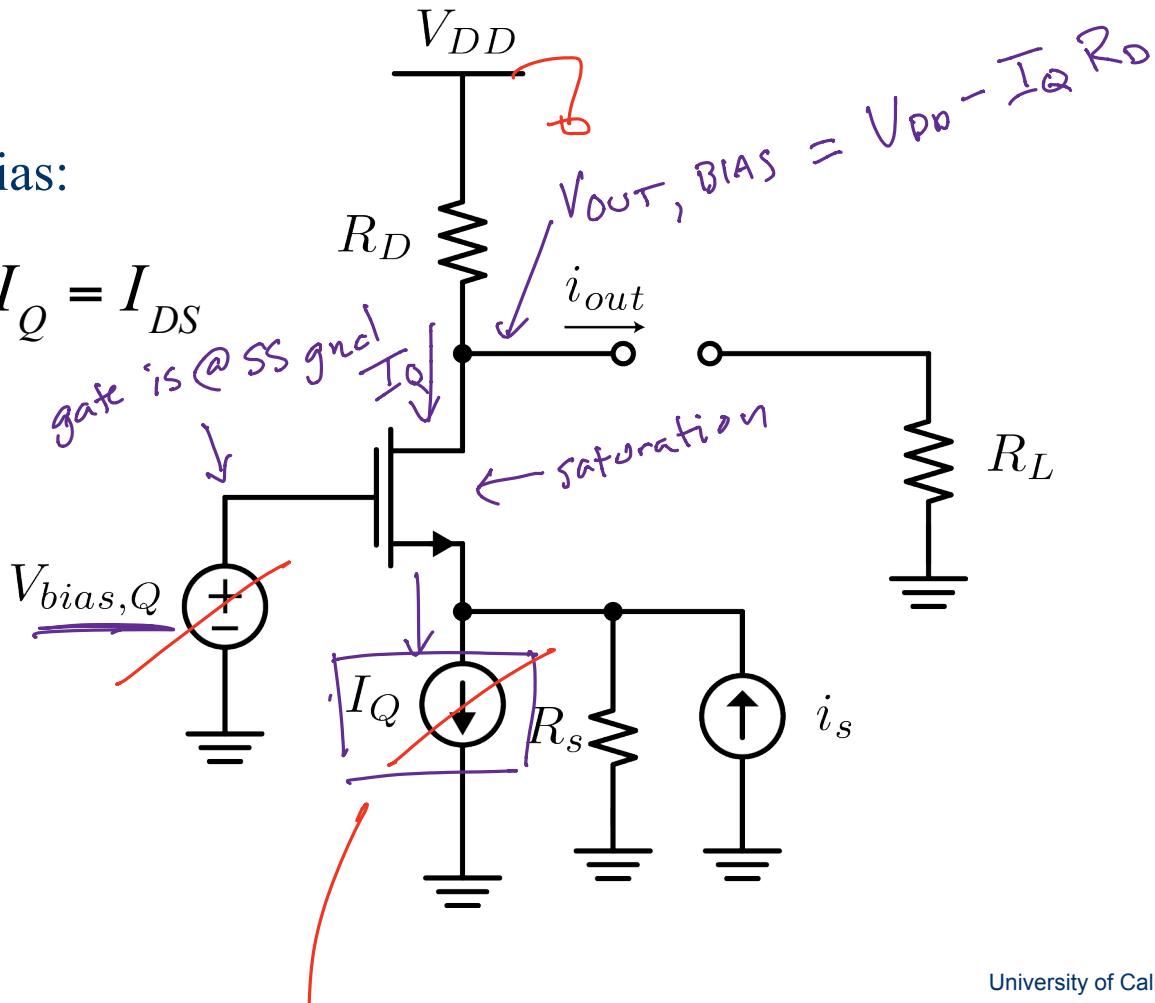


Common Drain (CD)

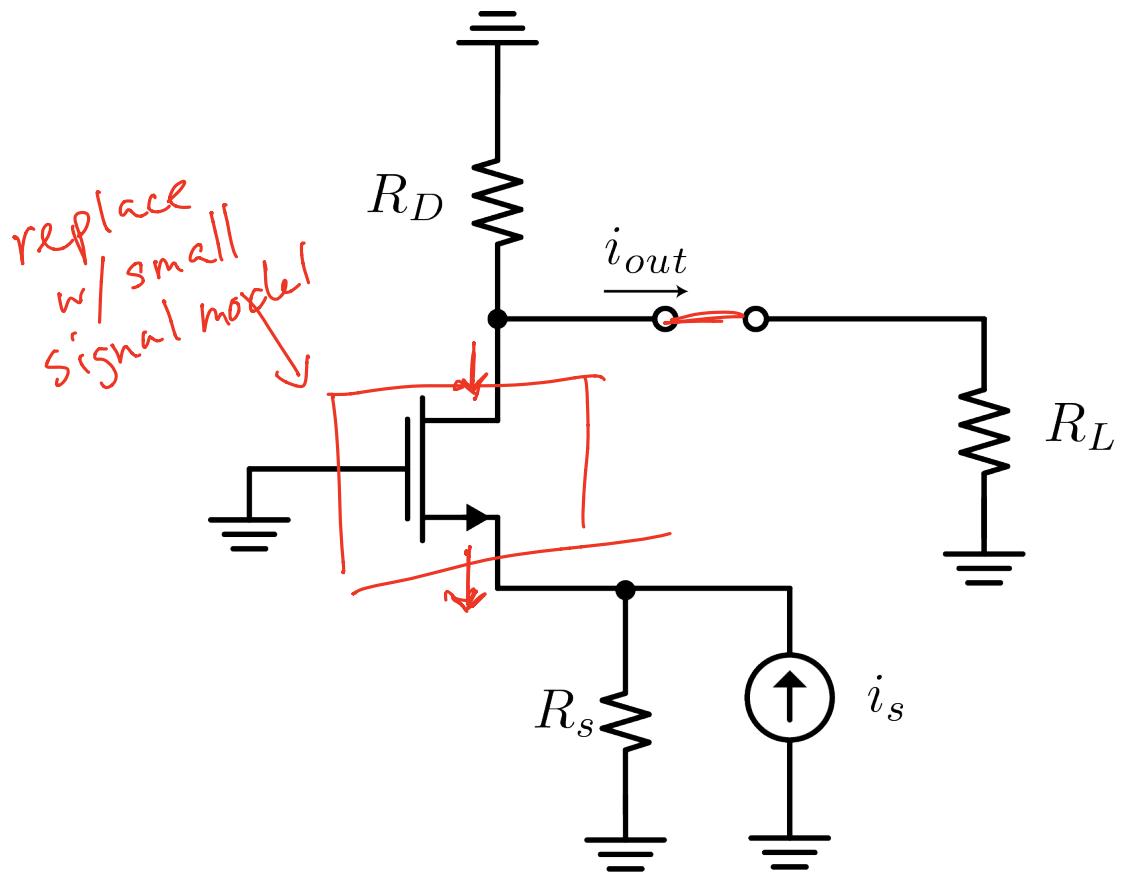
# Common Gate (CG) Amplifier

DC bias:

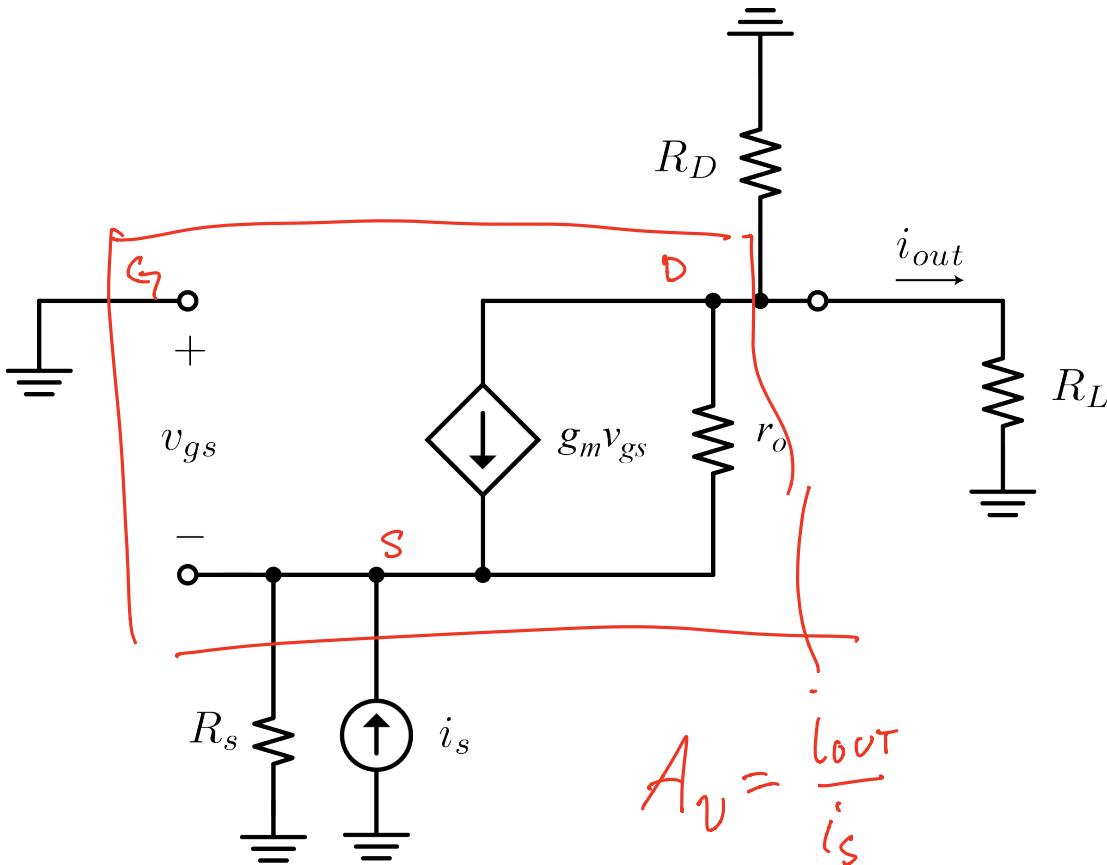
$$I_{SUP} = I_Q = I_{DS}$$



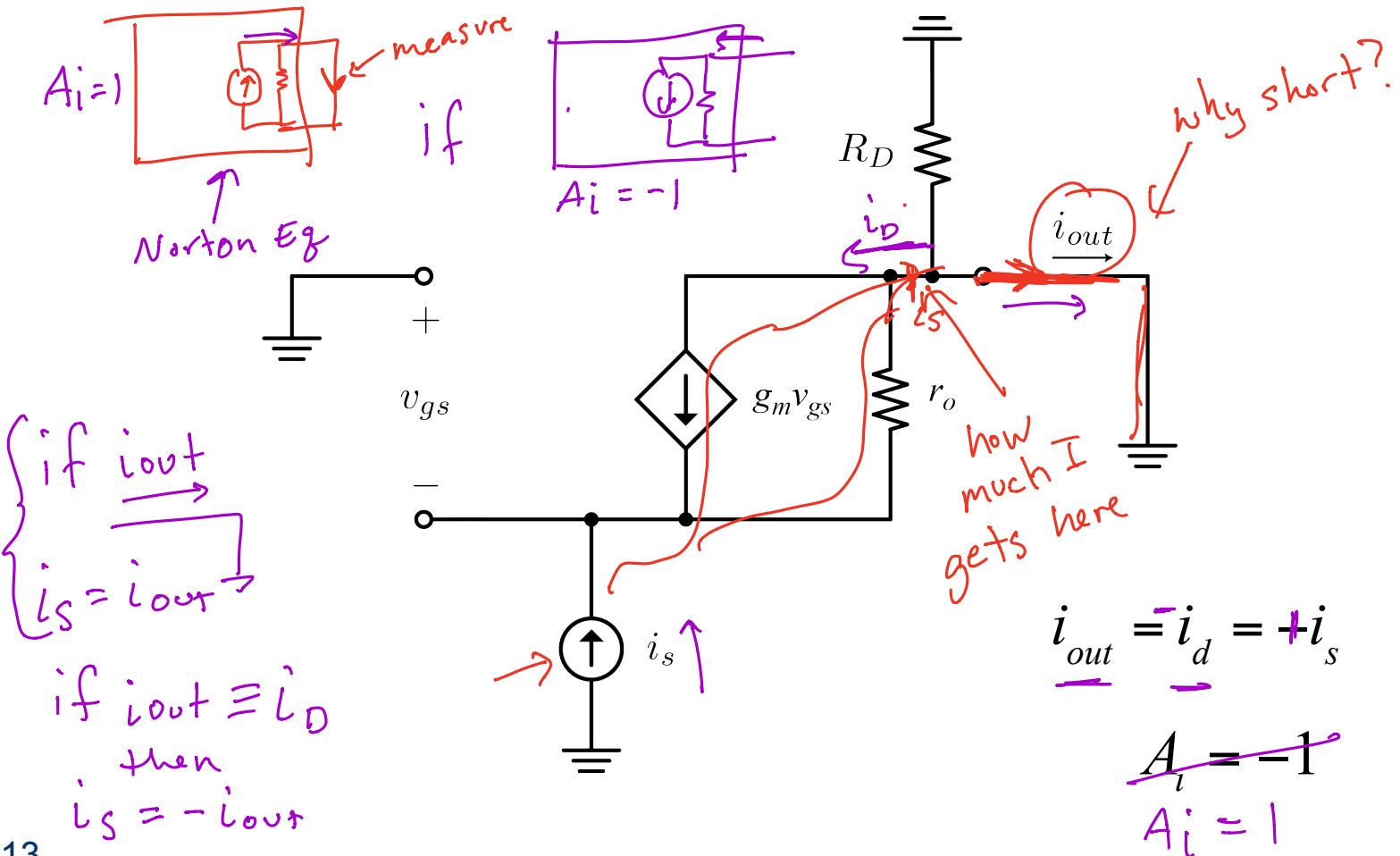
# Common Gate AC Model



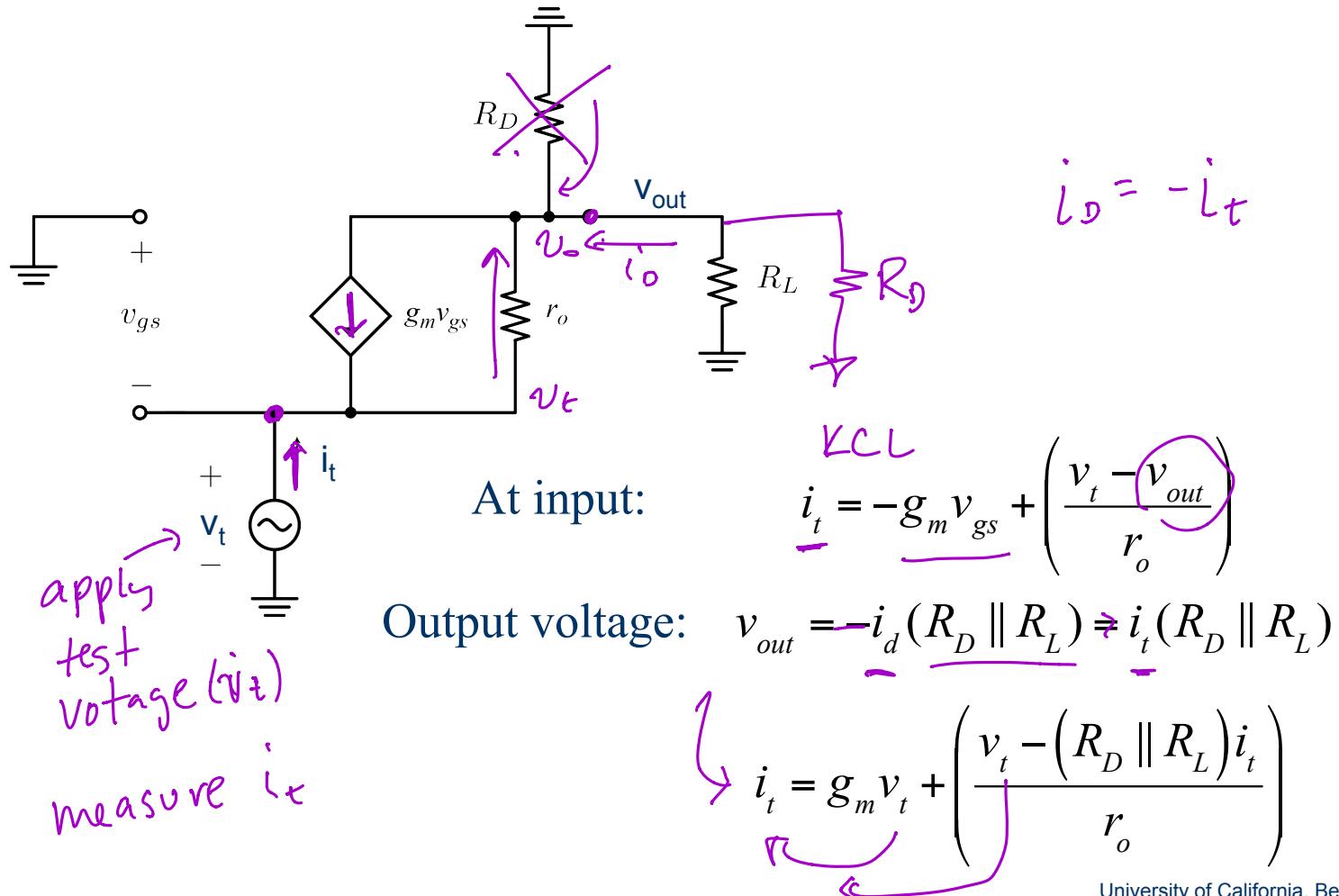
# Common Gate Small Signal



# CG as a Current Amplifier: Find $A_i$



# CG Input Resistance



# Approximations...

- We have this messy result

$$\left[ \frac{1}{R_{in}} \right] = \left[ \frac{i_t}{v_t} \right] = \frac{g_m + \frac{1}{r_o}}{1 + \frac{R_D \parallel R_L}{r_o}}$$

$\frac{1}{R_{in}} \approx g_m$

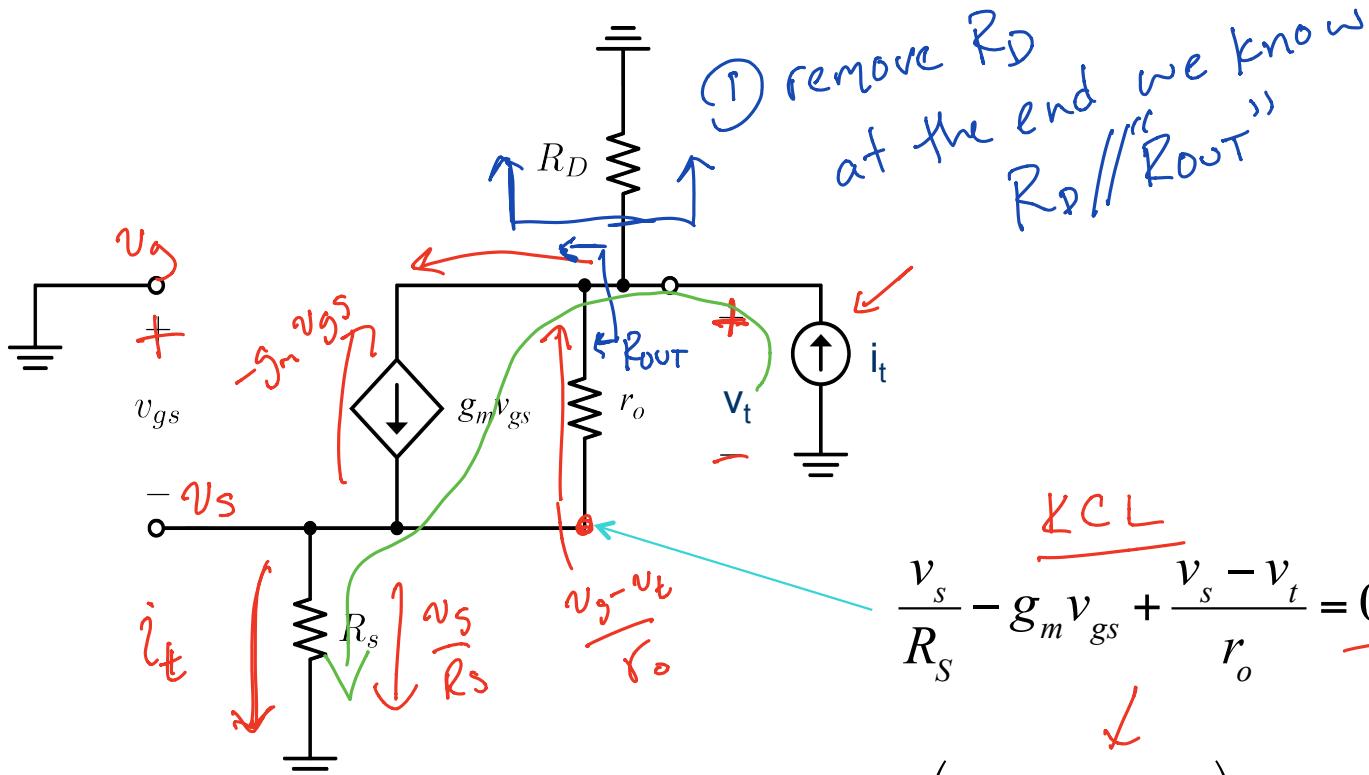
- But we don't need that much precision. Let's start approximating:

$g_m \gg \frac{1}{r_o}$        $R_D \parallel R_L \approx R_L$        $\frac{R_L}{r_o} \approx 0$

*r<sub>o</sub> is large*      *smaller*      *give you this information*

$R_{in} \approx \frac{1}{g_m}$       *small resistance*

# CG Output Resistance



$$\frac{v_s}{R_s} - g_m v_{gs} + \frac{v_s - v_t}{r_o} = 0$$

$$v_s \left( \frac{1}{R_s} + g_m + \frac{1}{r_o} \right) = \frac{v_t}{r_o}$$

# CG Output Resistance

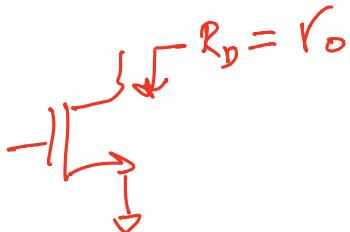
Substituting  $v_s = i_t R_S$

$$R_t = \frac{v_t}{i_t}$$

$$i_t R_S \left( \frac{1}{R_S} + g_m + \frac{1}{r_o} \right) = \frac{v_t}{r_o}$$

The output resistance is  $(v_t / i_t) \parallel \underline{R_D}$

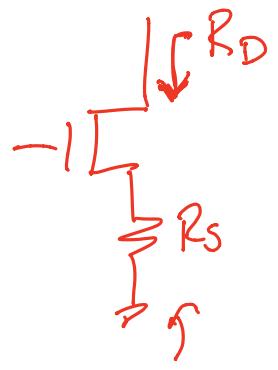
Bring  $R_D$   
back in



$$R_{out} = R_D \parallel \left( R_S \left( \frac{r_o}{R_S} + g_m r_o + 1 \right) \right)$$

$$R_{out} = R_D \parallel \left( \underline{r_o + g_m r_o R_S + R_S} \right)$$

resistance is  
large



source  
degeneration

# Approximating the CG $R_{out}$

The exact result is complicated, so let's try to make it simpler:

$$g_m \approx \underline{500 \mu S}$$

$$r_o \approx \underline{200 k\Omega}$$

$$R_{out} \cong R_D \parallel [r_o + g_m r_o R_S + \cancel{R_S}]$$

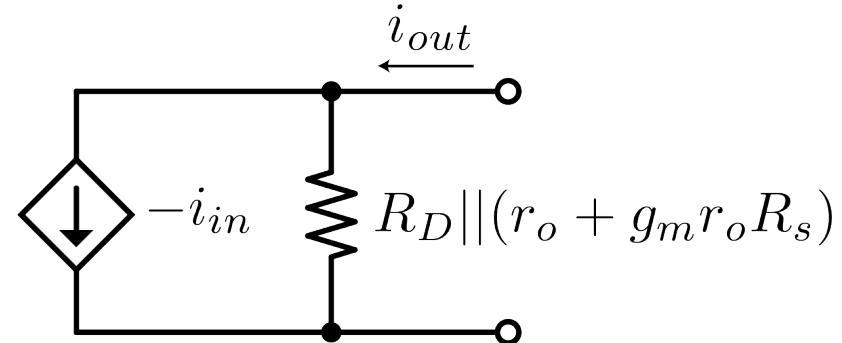
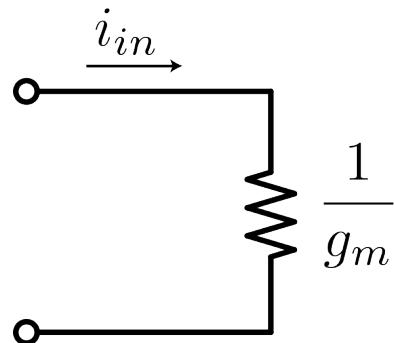
$\cancel{R_S} \ll r_o$

Assuming the source resistance is less than  $r_o$ ,

$$R_{out} \approx R_D \parallel \underline{[r_o + g_m r_o R_S]} = \underline{R_D} \parallel \underline{\underline{[r_o(1 + g_m R_S)]}}$$

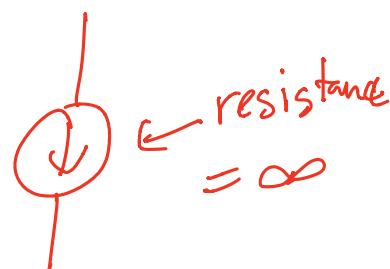
good approximation

# CG Two-Port Model

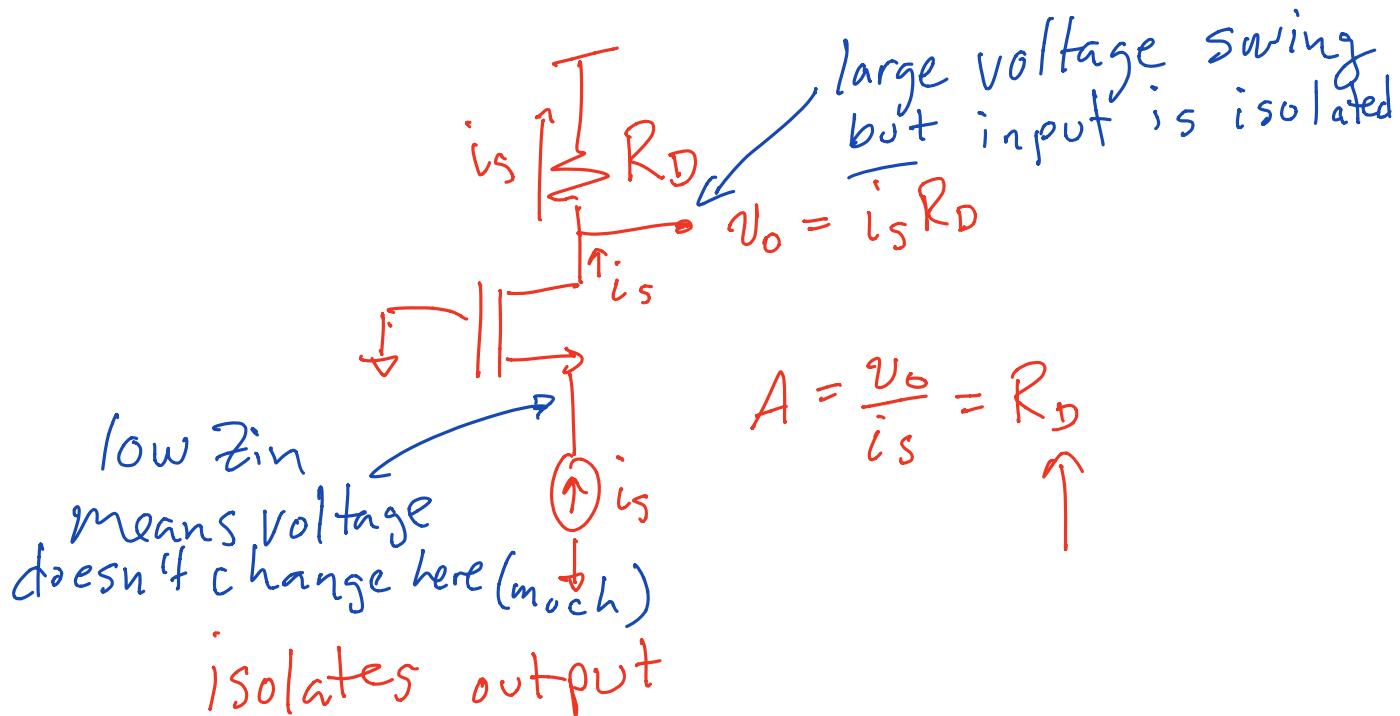


Function: a current buffer

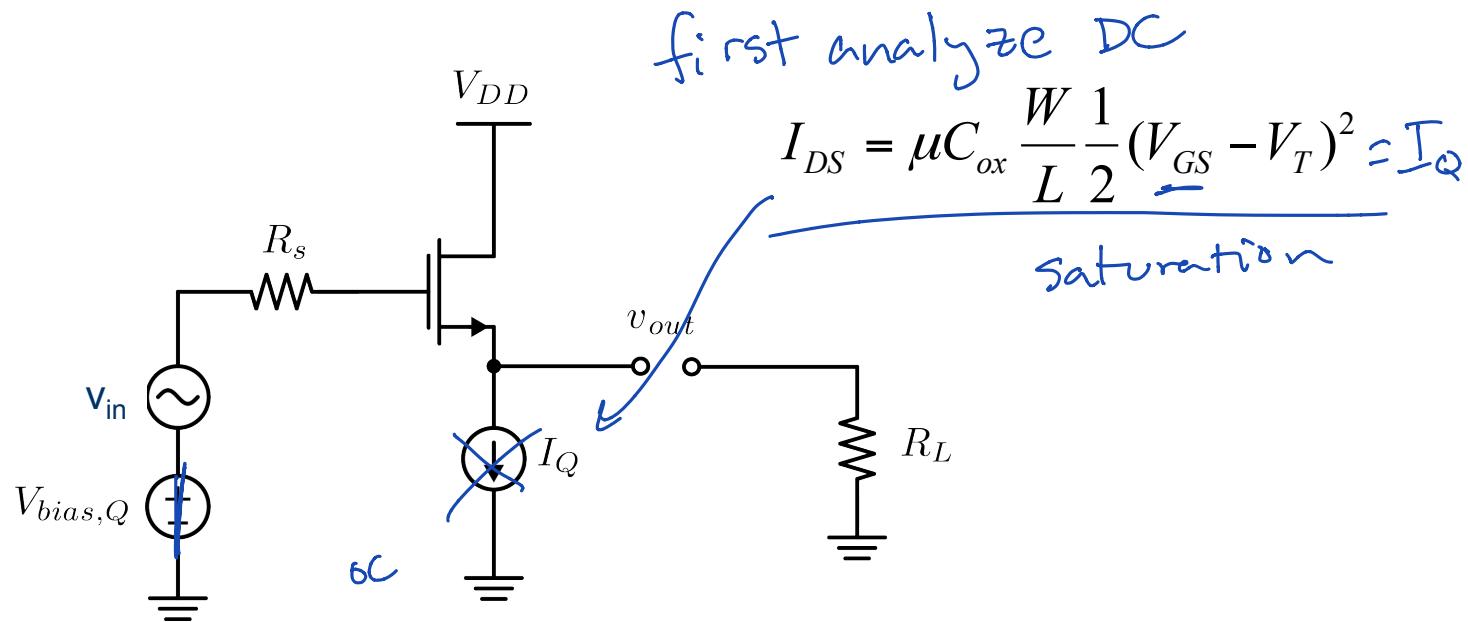
- Low Input Impedance
- High Output Impedance



# Common Gate as a “V Amplifier”



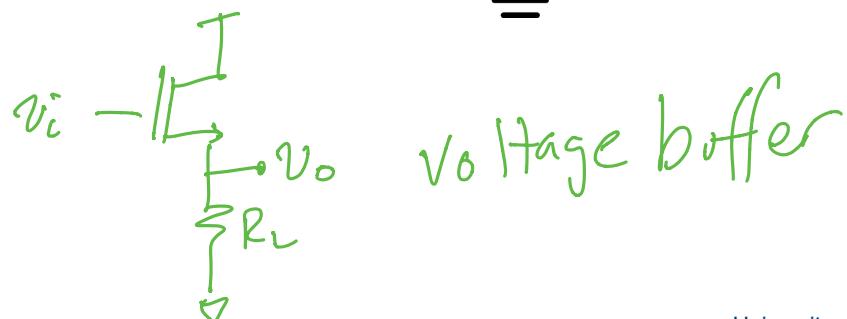
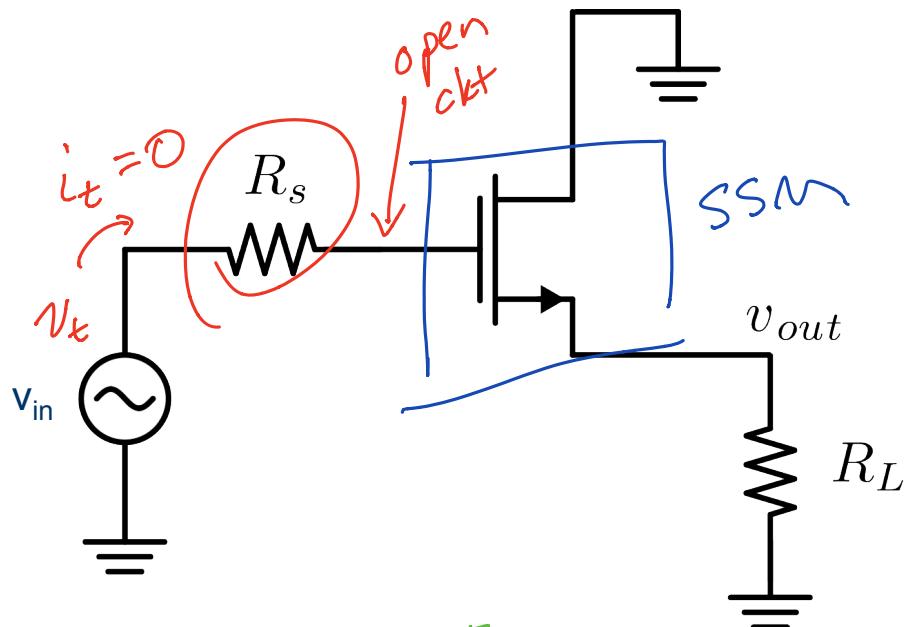
# Common-Drain Amplifier



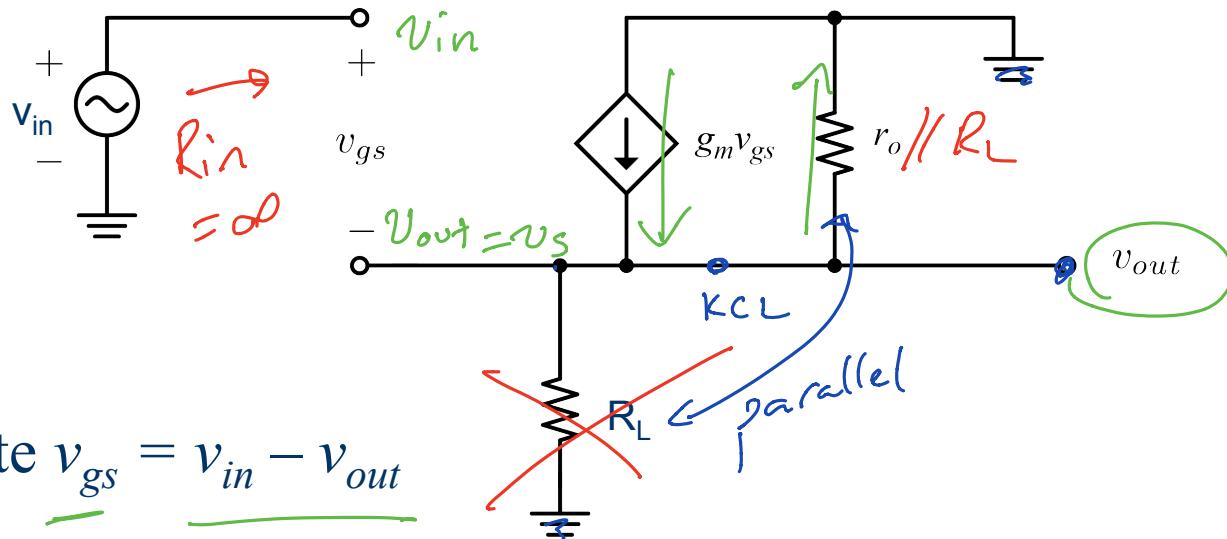
$$V_{GS} = V_T + \sqrt{\frac{2I_{DS}}{\mu C_{ox} \frac{W}{L}}} I_Q$$

Weak  $I_{DS}$  dependence

# Common Drain AC Schematic



# CD Voltage Gain



$$\frac{v_{out}}{R_L \parallel r_o} = g_m v_{gs}$$

$$\frac{v_{out}}{R_L \parallel r_o} = g_m (v_{in} - v_{out})$$

# CD Voltage Gain (Cont.)

KCL at source node:  $\frac{v_{out}}{R_L \parallel r_o} = g_m(v_{in} - v_{out})$

$$\left( \frac{1}{R_L \parallel r_o} + g_m \right) v_{out} = g_m v_{in}$$

Voltage gain:

want  $R_L$  large

$$\frac{v_{out}}{v_{in}} = \frac{g_m}{\frac{1}{R_L \parallel r_o} + g_m}$$

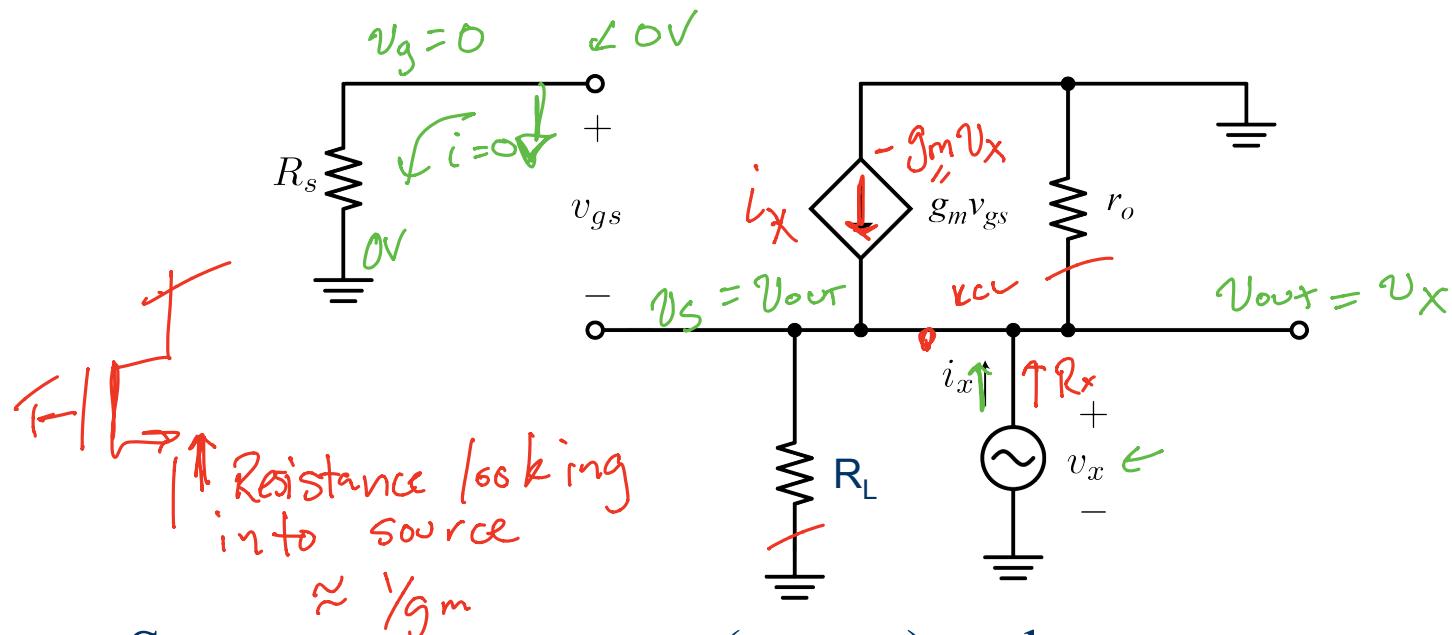
$$\frac{v_{out}}{v_{in}} \approx \frac{g_m}{1/R_L + g_m} \approx 1$$

$r_o \rightarrow$  large  
 $R_L \parallel r_o \approx R_L$

$g_m > \frac{1}{R_L}$  if  
 large

$\sim 0.97 \rightarrow$  always  $< 1$

# CD Output Resistance



Sum currents at output (source) node:

$$\underline{i_x = g_m v_x}$$

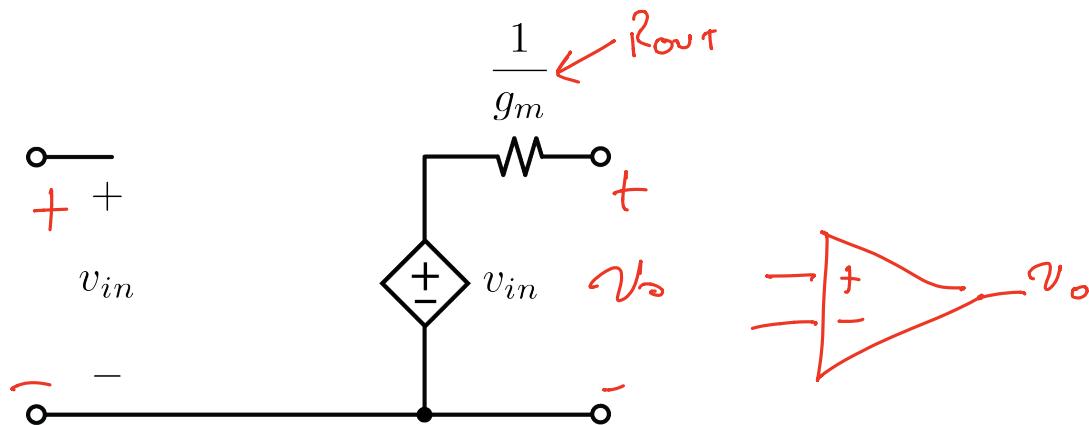
$$\underline{\frac{v_x}{i_x} = \frac{1}{g_m}}$$

$$R_{out} = r_o \parallel R_L \parallel \left( \frac{v_x}{i_x} \right) = \frac{1}{g_m}$$

$$\underline{R_{out} \approx \frac{1}{g_m}}$$

# CD Output Resistance (Cont.)

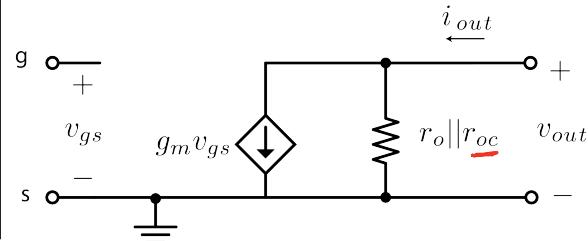
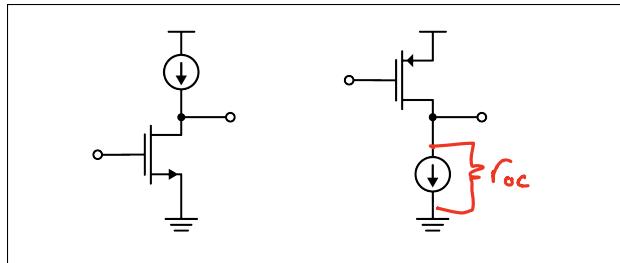
$r_o \parallel R_L$  is much larger than the inverses of the transconductances  $\rightarrow$  ignore



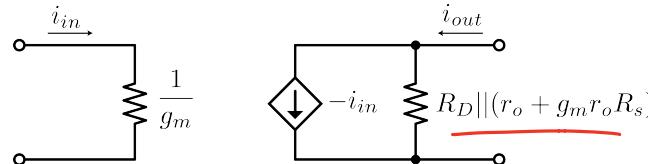
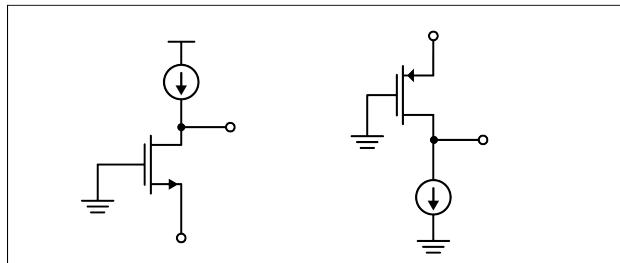
Function: a voltage buffer

- High Input Impedance
- Low Output Impedance

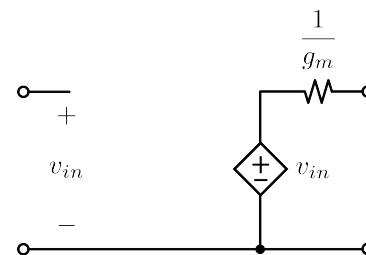
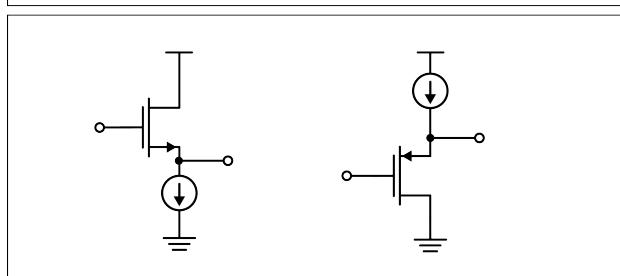
# Transistor Amplifiers → Gm/V/I



Gm  
Amplifier  
Common  
Source



I-Buffer  
Common  
Gate

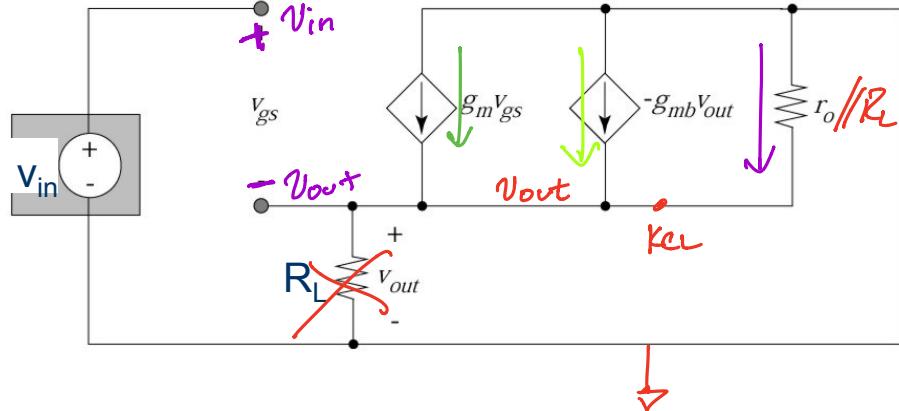
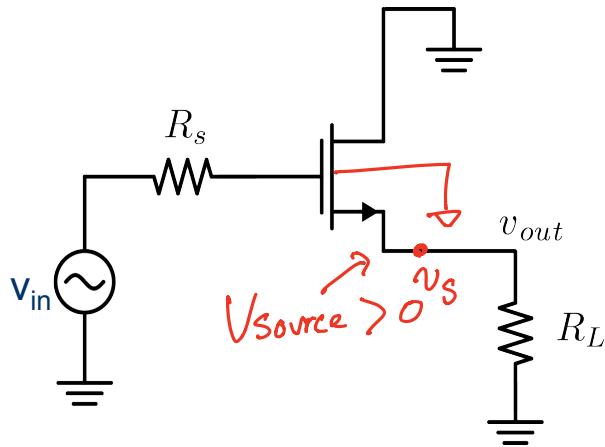


V-Buffer  
Source  
Follower

$$\text{Circuit symbol: } \begin{array}{c} + \\ | \\ - \end{array} \quad R_s \approx \frac{1}{g_m}$$

$$\text{Circuit symbol: } \begin{array}{c} + \\ | \\ - \end{array} \quad R_s \approx r_o (1 + g_m R_s)$$

# Body Effect



If the backgate is tied to ground you cannot ignore the body effect. How does this effect the gain?

$$\frac{v_{out}}{R_L \parallel r_o} = g_m v_{gs} - g_{mb} v_{out} - \frac{v_{out}}{R_L \parallel r_o} = 0$$

$$\frac{v_{out}}{v_{in}} = ?$$

$$\frac{v_{out}}{R_L \parallel r_o} + g_{mb} v_{out} = g_m v_{gs}$$

SSM

$$V_{bs} = V_b - V_s = 0 - v_{out}$$

$$v_{GS} = v_{in} - v_{out}$$

$$\frac{v_{out}}{R_L \parallel r_o} + g_m b v_{out} + g_m v_{out} = g_m v_{in}$$

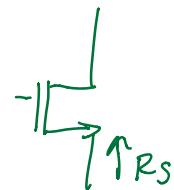
$$v_{out} \left( \frac{1}{R_L \parallel r_o} + g_m b + g_m \right) = g_m v_{in}$$

$$\frac{v_{out}}{v_{in}} = \frac{g_m}{\frac{1}{R_L \parallel r_o} + g_m b + g_m}$$

small

approximations

$$\frac{v_{out}}{v_{in}} \approx \frac{g_m}{g_m b + g_m}$$



$$\frac{1}{g_m}$$

$$\sim \frac{1}{g_m + g_m b}$$